

BHARATHIDASAN UNIVERSITY, TIRUCHIRAPPALL – 620 024

B.Sc. Physics / Chemistry / Industrial Electronics / Geology - Students

(For the candidates admitted from the academic year 2016-17 onwards)

ALLIED MATHEMATICS

ALLIED COURSE I

CALCULUS AND FOURIER SERIES

Objects :

1. To learn the basic need for their major concepts
2. To train the students in the basic Integrations

UNIT I

Successive Differentiation – n^{th} derivative of standard functions (Derivation not needed) simple problems only-Leibnitz Theorem (proof not needed) and its applications- Curvature and radius of curvature in Cartesian only (proof not needed)–Total differential coefficients (proof not needed) - Jacobians of two & three variables –Simple problems in all these.

UNIT II

Evaluation of integrals of types

$$\begin{array}{lll} 1] \int \frac{px+q}{ax^2+bx+c} dx & 2] \int \frac{px+q}{\sqrt{ax^2+bx+c}} dx & 3] \int \frac{dx}{(x+p)\sqrt{ax^2+bx+c}} \\ 4] \int \frac{dx}{a+b\cos x} & 5] \int \frac{dx}{a+b\sin x} & 6] \int \frac{(a\cos x+b\sin x+c)}{(p\cos x+q\sin x+r)} dx \end{array}$$

Integration by trigonometric substitution and by parts of the integrals

$$1] \int \sqrt{a^2-x^2} dx \quad 2] \int \sqrt{a^2+x^2} dx \quad 3] \int \sqrt{x^2-a^2} dx$$

UNIT III

General properties of definite integrals – Evaluation of definite integrals of types

$$1] \int_a^b \frac{dx}{\sqrt{(x-a)(b-x)}} \quad 2] \int_a^b \sqrt{(x-a)(b-x)} dx \quad 3] \int_a^b \sqrt{\frac{x-a}{b-x}} dx$$

Reduction formula (When n is a positive integer) for

$$\begin{array}{lll} 1] \int_a^b e^{ax} x^n dx & 2] \int_a^b \sin^n x dx & 3] \int_a^b \cos^n x dx \end{array}$$

$$4] \int_0^x e^{ax} x^n dx \qquad 5] \int_0^{\frac{\pi}{2}} \sin^n x dx$$

$$6] \text{ Without proof } \int_0^{\frac{\pi}{2}} \sin^n x \cos^m x dx - \text{ and illustrations}$$

UNIT IV

Evaluation of Double and Triple integrals in simple cases –Changing the order and evaluating of the double integration. (Cartesian only)

UNIT V

Definition of Fourier Series – Finding Fourier Coefficients for a given periodic function with period 2π and with period 2ℓ - Use of Odd & Even functions in evaluating Fourier Coefficients - Half range sine & cosine series.

TEXT BOOK(S)

1. S. Narayanan, T.K. Manichavasagam Pillai, Calculus, Vol. I, S. Viswanathan Pvt Limited, 2003
2. S. Arumugam, Isaac and Somasundaram, Trigonometry & Fourier Series, New Gamma Publishers, Hosur, 1999.

ALLIED COURSE II

ALGEBRA, ANALYTICAL GEOMETRY (3D) AND TRIGONOMETRY

Objects :

1. To learn the basic concepts of Algebra
2. To learn the basic needs Trigonometry

UNIT I

Binomial, Exponential and Logarithmic series (Formulae only) – summation & approximation related problems only.

UNIT II

Non-Singular , Symmetric , Skew symmetric, Orthogonal, Hermitian, Skew Hermitian and Unitary matrices – Characteristic equation , eigen values, eigen vectors – Cayley Hamilton's Theorem (proof not needed) –Simple applications only.

UNIT III

Finding the Shortest distance between two skew lines and the equation of the plane containing them– Condition for Coplanarity – Equation of a Sphere – Tangent plane – Plane section of a sphere.- Finding the center & radius of the circle of intersection – Sphere through the circle of intersection (only problems in all the above)

UNIT IV

Expansion of $\sin n\theta$, $\cos n\theta$, $\tan n\theta$ (n being a positive integer) - Expansion of $\sin^n \theta$, $\cos^n \theta$, $\sin^n \theta \cos^m \theta$ in a series of sines & cosines of multiples of θ (θ - given in radians) - Expansion of $\sin \theta$, $\cos \theta$ and $\tan \theta$ in terms of powers of θ (only problems in all the above).

UNIT V

Euler's formula for $e^{i\theta}$ - Definition of Hyperbolic functions –Formulae involving Hyperbolic functions -Relation between Hyperbolic & circular functions – Expansion of $\sinh x$, $\cosh x$, $\tanh x$ in powers of x - Expansion of Inverse hyperbolic functions $\sinh^{-1} x$, $\cosh^{-1} x$ and $\tanh^{-1} x$ -Separation of real & imaginary parts of $\sin(x+iy)$, $\cos(x+iy)$, $\tan(x+iy)$, $\sinh(x+iy)$, $\cosh(x+iy)$, $\tanh(x+iy)$

TEXT BOOK(S)

1. T.K. Manicavachagam Pillai, T. Natarajan, K.S. Ganapathy, Algebra, Vol. I, S. Viswanathan Pvt Limited, Chennai, 2004
2. S. Narayanan, T.K. Manichavasagam Pillai, S. Viswanathan Pvt Limited, and Vijay Nicole Imprints Pvt Ltd, 2004.
3. T.K.Manickavasagam Pillai, Analytical Geometry (3D) and Vector Calculus, New Gamma Publishing House, 1991.

ALLIED COURSE III

ODE, PDE, LAPLACE TRANSFORMS AND VECTOR ANALYSIS

Objects :

1. To learn the basic needs for their major concepts
2. To train the students in PDE and Laplace Transforms

UNIT I

Ordinary Differential Equation of first order but of higher degree –Equations solvable for x , solvable for $\frac{dy}{dx}$, Clairaut's form (simple cases only) – Linear equations with constant coefficients – Finding Particular integrals in the cases of e^{kx} , $\sin(kx)$, $\cos(kx)$ (where k is a constant) , x^k where k is a positive integer , and $e^{kx} f(x)$ where $f(x)$ is any function of x -(only problems in all the above –No proof needed for any formula).

UNIT II

Formation of Partial differential equations by eliminating constants and by elimination of arbitrary functions – definition of general , particular & complete solutions – Singular integral (geometrical meaning not required) – Solutions of first order equations in the standard forms- $f(p, q) = 0$, $f(x, p, q) = 0$, $f(y, p, q) = 0$, $f(z, p, q) = 0$, $f_1(x, p) = f_2(y, q)$, $z = xp + yq + f(p, q)$ – Lagrange's method of solving $Pp + Qq = R$,where P, Q, R are functions of x, y, z – (Geometrical Meaning is not needed)- (only problems in all the above – No proof needed for any formula).

UNIT III

Laplace Transform – Definition – $L(e^{at})$, $L(\cos(at))$, $L(\sin(at))$, $L(t^n)$, where n is a positive integer. Basic theorems in Laplace Transforms (formula only)- $L[e^{-st} \cos bt]$, $L[e^{-st} \sin bt]$, $L[e^{-st} f(t)] = L[f(t)]$, $L[f'(t)]$, $L[f''(t)]$ –

UNIT IV

Inverse Laplace Transforms related to the above standard forms – Solving Second Order ODE with constant coefficients using Laplace Transforms.

UNIT V

Gradient of a vector – directional derivative – unit normal vector - tangent plane – Divergence-Curl – solenoidal & irrotational vectors – Double operators - Properties connecting grad., div., and curl of a vector.

TEXT BOOK(S)

1. S.Narayanan, Differential Equations, S. Viswanathan Publishers, 1996.
2. S. Narayanan, T.K. Manicavachagam Pillai, Calculus, Vol. II, S. Viswanathan Pvt Limited, 2003
3. M.L. Khanna, Differential Calculus, Jaiprakashnath and Co., Meerut-2004.

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**B.Sc. Computer Science, B.Sc. Information Technology, BCA &
B.Sc. Software Development Programmes**

ALLIED MATHEMATICS

ALLIED COURSE I

ALGEBRA AND CALCULUS

Objects :

1. To learn the basic concepts in the integration
2. To train the students to solve the problems in Theory of Equations

UNIT I

Theory of Equations: Relation between roots & coefficients – Transformations of Equations – Diminishing, Increasing & multiplying the roots by a constant- Forming equations with the given roots –Rolle's Theorem, Descartes's rule of Signs(statement only) –simple problems.

UNIT II

Matrices : Singular matrices – Inverse of a non-singular matrix using adjoint method - Rank of a Matrix – Consistency - Characteristic equation, Eigen values, Eigen vectors – Cayley Hamilton's Theorem (proof not needed) –Simple applications only

UNIT III

Differentiation: Maxima & Minima – Concavity, Convexity – Points of inflexion - Partial differentiation – Euler's Theorem - Total differential coefficients (proof not needed) –Simple problems only.

UNIT IV

Integration : Evaluation of integrals of types

$$\begin{array}{lll} 1] \int \frac{px+q}{ax^2+bx+c} dx & 2] \int \frac{px+q}{\sqrt{ax^2+bx+c}} dx & 3] \int \frac{dx}{a+b \sin x} \\ 4] \int \frac{dx}{a+b \cos x} \end{array}$$

Evaluation using Integration by parts – Properties of definite integrals – Fourier Series in the range (0 , 2 π) – Odd & Even Functions – Fourier Half range Sine & Cosine Series

UNIT V

Differential Equations: Variables Separables – Linear equations – Second order of types $(aD^2 + bD + c)y = F(x)$ where a, b, c are constants and $F(x)$ is one of the following types (i) e^{Kx} (ii) $\sin(kx)$ or $\cos(kx)$ (iii) x^n , n being an integer (iv) $e^{Kx} f(x)$

TEXT BOOK(S)

1. T.K. Manickavasagam Pillai & others, Algebra, Volume I, S.V Publications, 1985 Revised Edition (Units I, II)
2. S. Narayanan, T.K. Manicavachagam Pillai, Calculus, Vol. II, S. Viswanathan Pvt Limited, 2003. (Units III, IV and V)

REFERENCE(S)

1. M.L. Khanna, Differential Calculus, Jaiprakashnath and Co., Meerut-2004.

ALLIED COURSE II

NUMERICAL ANALYSIS AND STATISTICS

Objects :

1. To train the students in the numerical problems
2. To train the students in solving statistical problems

UNIT I

Algebraic & Transcendental equations : Bisection Method , Newton Raphson Method , Iteration method - Finite differences –Forward , Backward differences – Newton's forward & backward difference interpolation formulae. Lagrange's interpolating polynomial.

UNIT II

Numerical differentiation - Numerical Integration using Trapezoidal rule and Simpson's first & second rules (proof not needed) - Solutions to Linear Systems – Gaussian Elimination Method – Jacobi & Gauss Seidel iterative methods – Theory and problems

UNIT III

Numerical solution of ODE : Solution by Taylor Series Method , Euler's Method, Runge - Kutta 2nd order method- Adam's Predictor Corrector Method and Milne's Predictor Corrector Methods

UNIT IV

Arithmetic Mean – Geometric Mean – Harmonic Mean - Median, Mode , Standard Deviation - Quartile Deviation – Percentiles - Expectation – Variance and covariance –

UNIT V

Correlation and Regression –Properties of Simple Correlation and regression coefficients – Simple Numerical Problems only.

TEXT BOOK(S)

1. S.S.Sastry, Numerical Analysis (Unit 1 , 2 , 3)
2. Gupta.S.C & Kapoor, V.K, Fundamentals of Mathematical Statistics, Sultan Chand & sons, New Delhi -1994. (Units 4 & 5)

REFERENCE(S)

1. M.K. Jain, S.R.K. Iyengar and R.K. Jain, Numerical Methods for Scientific and Engineering Computation, New Age International Private Limited, 1999.
2. C.E. Froberg, Introduction to Numerical Analysis, II Edn., Addison Wesley, 1979.

ALLIED COURSE III
OPERATIONS RESEARCH

Objects :

1. To train the students to solve assignment problems, transportation problems
2. To train the students in network problems.

UNIT I

Operations Research : Introduction - Basics of OR – OR & decision making – Role of Computers in OR - Linear programming formulations & graphical solution of two variables – Canonical & standard forms of LPP

UNIT II

Simplex Method : Simplex Method for $<$, $=$, $>$ constraints – Charne's method of penalties– Two phase Simplex method.

UNIT III

Transportation problem : Transportation algorithm –Degeneracy algorithm – Degeneracy in Transportation Problem , Unbalanced transportation problem- Assignment algorithm –Unbalanced Assignment problem .

UNIT IV

Sequencing problem : Processing of n jobs through two machines – Processing of n jobs through 3 machines – processing of two jobs through m machines.

UNIT V

Networks: Network – Fulkerson's rule - measure of activity – PERT computation – CPM computation - Resource scheduling.

TEXT BOOK(S)

1. Manmohan & Gupta , Operations Research, Sultan Chand Publishers, New Delhi

REFERENCE(S)

1. Prem Kumar Gupta and D.S. Hira, Operations Research : An Introduction, S. Chand and Co., Ltd. New Delhi,
2. Hamdy A. Taha, Operations Research (7th Edn.), McMillan Publishing Company, New Delhi, 1982.

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MATHEMATICAL STATISTICS

(For the candidates admitted from the academic year 2016-17 onwards)

ALLIED COURSE I

Objectives

1. To learn the basic concepts of statistics
2. To learn the basic ideas of statistical datas

Unit I

Statistical data – Primary data and Secondary data(definitions only), Formation of frequency distribution, various measures of central tendency – mean ,median, mode, geometric mean harmonic mean – simple problems – properties of above measures.

Unit II

Measures of dispersion – Range quartile deviation mean deviation, standard deviation – their coefficients- merits and demerits (simple problems) – Skewness and kurtosis- Karlpearson's coefficients- Bowley's coefficients- simple problems

Unit III

Probability- Definition, axiomatic approach to probability - Additive and Multiplicative laws of Probability (two variables only) and Conditional probability – simple problems- Concept of random variables – discrete and continuous random variables - Distribution function, pmf and pdf and their properties- simple problems.

Unit IV

Mathematical Expectation – addition and multiplication theorems (two variables only). Moment generating and characteristic functions, their properties. Conditional expectation and conditional variance (simple problems).

Unit V

Binomial and poisson distributions – moments, moment generating function cumulant generating function (Simple problems)- fitting binomial distribution and gamma distribution.

Books for Study:

1. Gupta S.C. and Kapoor V.K. : Fundamentals of Mathematical Statistics – Sultan Chand & Sons.
2. S.P. Gupta , Statistical Methods (Revised edition 2001)
3. R.S.N. Pillai and Bagavathi , Practical statistics, Second edition (2013)

Reference:

1. Gupta S.C. and Kapoor V.K. : Fundamentals of Applied Statistics – Sultan Chand & Sons.

MATHEMATICAL STATISTICS

ALLIED PRACTICAL

25 marks for records and 75 marks for Practical Examination

Passing minimum for Record – 10 marks (out of 25 marks)

Practical Examination – 30 marks (out of 75 marks)

Objectives:

To train the students in solving statistical problems

Unit I

Moments of central tendency- A.M, median, G.M and H.M- Measures of Dispersion- quartile deviation, standard deviation and co-efficient of variation- measures of skewness - calculations of first four moments, Central moments, B_1 , B_2 .

Unit II

Bivariate discrete probability distribution- marginal distribution and conditional distribution –Calculation of mean, variance, covariance, correlation coefficient, expectation - conditional expectations and conditional variance.

Unit III

Fitting of binomial, poisson and normal distributions (area method only).

Unit IV

Calculation of Karl pearson's coefficient of correlation, Spearman's rank correlation and regression equations.

Unit V

Large sample tests- Test of single mean- Difference between means – single proposition and Difference between proposition.

Exact sample test- t' test for single mean, Difference between means, paired t - test chisquar test for goodness of fit and independance of attributes.

Text Book:

- 1 Gupta S.C. and Kapoor V.K. : Fundamendals of Mathematical Statistics – Sultan Chand & Sons.
- 2 R.S.N. Pillai and Bagavathi ,Practical statistics, Second edition (2013)

MATHEMATICAL STATISTICS

ALLIED COURSE II

Objectives:

1. To learn the basic concepts of Discrete continuous distributions
2. To learn the test of significance

Unit I

Normal distribution – constants. m , g , f , binomial poisson and chisquare distribution tending to normal statement of central limit theorem. Characteristics functions and its properties. Statement of uniqueness theorem and continuity theorems.

Unit II

Continuous distributions – rectangular, exponential, Beta Gamma – distributions sampling distributions, 't' 'F' and chisquare distributions.

Unit III

Correlation – Rank correlation, Karl Pearson's correlation co-efficient and its properties. Linear regression and its properties, concept of multiple and partial correlation for three variables only.

Unit IV

Test of significance – Definition of null hypothesis, alternative hypothesis, sampling distribution, standard error and critical region. Type I and Type II errors, one tailed and two tailed tests. Large sample test for single mean, Difference between means, single proportion and difference between proportions.

Unit V

Small sample tests – 't' test for single mean. Difference between means. Paired 't' test, Chi- square test for goodness of fit and independence of attributes.

Text Books

1. Gupta, S.C. and Kapoor, V K – Fundamentals of Mathematical Statistics, Sultan Chand and Sons.
2. S.P. Gupta , Statistical Methods (Revised edition 2001)

ALLIED COURSE I

CALCULUS, LAPLACE TRANSFORM AND FOURIER SERIES

Objects :

1. To train the students in basic calculus
2. To learn the basic ideas of Fourier Series

UNIT I

Maxima & Minima – Concavity , Convexity – Points of inflexion - Partial differentiation – Euler’s Theorem - Total differential coefficients (proof not needed) –Simple problems only.

UNIT II

Evaluation of integrals of types

$$\begin{array}{lll} 1] \int \frac{px+q}{ax^2+bx+c} dx & 2] \int \frac{px+q}{\sqrt{ax^2+bx+c}} dx & 3] \int \frac{dx}{(x+p)\sqrt{ax^2+bx+c}} \\ 4] \int \frac{dx}{a+b\cos x} & 5] \int \frac{dx}{a+b\sin x} & 6] \int \frac{(a\cos x+b\sin x+c)}{(p\cos x+q\sin x+r)} dx \end{array}$$

Evaluation using Integration by parts

Integration by trigonometric substitution and by parts of the integrals

$$1] \int \sqrt{a^2-x^2} dx \quad 2] \int \sqrt{a^2+x^2} dx \quad 3] \int \sqrt{x^2-a^2} dx$$

UNIT III

General properties of definite integrals – Evaluation of definite integrals of types

$$1] \int_a^b \frac{dx}{\sqrt{(x-a)(b-x)}} \quad 2] \int_a^b \sqrt{(x-a)(b-x)} dx \quad 3] \int_a^b \sqrt{\frac{x-a}{b-x}} dx$$

Other simple problems. - Evaluation of Double and Triple integrals in simple cases Changing the order and evaluation of the double integration – Beta, Gamma functions.

UNIT IV

Laplace Transforms – Inverse Laplace Transforms –Application of Laplace Transform in Solving second order Ordinary differential equation with constant coefficients.

UNIT V

Definition of Fourier Series – Fourier Coefficients for a given periodic function with period 2π and with period 2ℓ - Use of Odd & Even functions in evaluating Fourier Coefficients– Half range sine & cosine series.

TEXT BOOK(S)

1. S. Narayanan, T.K. Manichavasagam Pillai, Calculus, Vol. II, S. Viswanathan Pvt Limited, 2003
2. S. Narayanan, T.K. Manicavachagam Pillai, Calculus, Vol. III, S. Viswanathan Pvt Limited, and Vijay Nicole Imprints Pvt Ltd, 2004.

ALLIED COURSE II

ALGEBRA

Objects :

1. To learn the basic ideas of vector spaces
2. To learn the basic ideas of rank and linear transformation

UNIT I

Binomial, Exponential and Logarithmic series (Formulae only) – summation and approximation related problems only.

UNIT II

Non-Singular , Symmetric , Skew symmetric, Orthogonal, Hermitian, Skew Hermitian and Unitary matrices – simple properties & problems –Inverse of a non-singular matrix using adjoint method

UNIT III

Rank of a Matrix – Consistency - Characteristic equation , eigen values ,eigen vectors – Cayley Hamilton's Theorem (proof not needed) –Simple applications only

UNIT IV

Vector spaces and its properties –linear independence –Basis & Dimension - Subspaces

UNIT V

Linear transformation and its properties –Rank & nullity .

TEXT BOOK(S)

1. T.K. Manichavasam Pillai, T. Natarajan, K.S. Ganapathy, Algebra, Vol. I, S. Viswanathan Pvt Limited, Chennai, 2004 (Unit 1)
2. A.R. Vasistha, Matrices, Krishna Prakeshan Mandir, 24th Edition, 1994-95 (Unit 2 & 3)
3. M.L.Santiago, Modern Algebra (Unit 4 & 5), Arul Publications, Madras, 1993.

REFERENCE(S)

1. Narayanan, T.K. Manicavachagam Pillai & Ramnath, Advanced Mathematics for Engineers & Scientists, S. Viswanathan Publishers Pvt. Ltd., 1994

ALLIED COURSE III

ANALYSIS AND THEORY OF EQUATIONS

Objects :

1. To learn the basic ideas of sequences
2. To learn the basic ideas of series

UNIT I

Theory of equations-formation of equations- irrational and imaginary roots – relation between Roots & coefficients –Reciprocal equations –Reducing roots by a number –multiplying roots by a number

UNIT II

Real Number system – Absolute value of a real number – definition of supremum (LUB) and Infimum (GLB) – Limit of a function .

UNIT III

Definition of a sequence – Convergence and divergence of a sequence – Bounded sequences –Monotonic sequence –Algebra of sequences.

UNIT IV

Convergence and divergence of a series –Geometric series –simple tests for convergence of a Series (Comparison tests, ratio test, root test, Leibnitz test) – conditional convergence and absolute convergence of alternating series – Simple problems.

UNIT V

Continuous function and its properties – (Simple theorems only) – Uniform Continuity – Rolle's Theorem – Mean Value Theorem – Taylor's Theorem – Maclaurin Series.

TEXT BOOK(S)

1. T.K. Manicavachagam Pillai, Analysis, S.V. Publications, Chennai, 1985 (Unit 1 & 2)
2. Malik S.C, Mathematical Analysis, Wiley Eastern, New Delhi, 1984.
